

## Dividing Radical Expressions

### The Quotient Rule for Radicals (pg. 455 – 456)

For any real numbers  $\sqrt[n]{a}$  and  $\sqrt[n]{b}$  and  $b \neq 0$  then  $\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$

### Examples:

Simplify

$$\sqrt[3]{\frac{27}{125}}$$

$$\sqrt{\frac{25}{y^2}}$$

$$\sqrt{\frac{16x^3}{y^8}}$$

$$\sqrt[3]{\frac{27y^{14}}{8x^3}}$$

Divide and, if possible, simplify

$$\frac{\sqrt{80}}{\sqrt{5}}$$

$$\frac{5\sqrt[3]{32}}{\sqrt[3]{2}}$$

$$\frac{\sqrt{72xy}}{2\sqrt{2}}$$

$$\frac{\sqrt[4]{18a^9b^5}}{\sqrt[4]{3b}}$$

### Rationalizing Denominators or Numerators with one Term (pg. 457)

**Rationalizing the denominator or numerator** means to write the expression as an equivalent expression but without a radical in the denominator or numerator.

To do this multiply by 1 under the radical to make the denominator of the radicand a perfect power or multiply by 1 outside the radical.

**Examples:** Rationalize the denominator

$$\sqrt{\frac{7}{3}}$$

$$\sqrt[3]{\frac{5}{16}}$$

$$\sqrt{\frac{4}{5b}}$$

$$\frac{\sqrt[3]{a}}{\sqrt[3]{25bc^5}}$$

$$\frac{3x}{\sqrt[5]{2x^2y^3}}$$

Rationalize the numerator

$$\frac{\sqrt[3]{4a^2}}{\sqrt[3]{5b}}$$